Probability & simulations

Simulation : randint(a,b,n)

a dice	randint(1,6,n)
a coin	randint(0,1,n) <i>sum(randint(0,1,n))</i>
a family	randint(0,1,n) <i>sum(randint(0,1,n))</i>

Transport your result to a spreadsheet :

randint(1,6,10) ; enter CTRL *var* and type *d* ; enter

< 1.1 1.2 ▶	*Doc 🗢	grad 🚺 🗙
randInt(1,6,10)	{ 6,6,1,4	,3,5,1,3,6,2 }
{6,6,1,4,3,5,1,3,6,	$2 \} \rightarrow d$	
	{ 6,6,1,4	,3,5,1,3,6,2}

Open a spreadsheet and name your column *d* ; enter.

•	1.1 1.2 🕨	*Doc <	7	🔓 grad 🚺	X
P	A d	В	С	D	I
=					
1	6				
2	6				
3	1				
4	4				
5	3				
G4				•	

Or use the formula bar in your spreadsheet :

1	1.1 1.2 2	.1 🕨 *Doc 🗸	~	🗟 GRAD 🕻	
P	A	в	С	D	
=	=randint(1				
1	6				
2	2				
3	2				
4	1				
5	1				
A =	=randint(1,6	5,10)		•	

EXAMPLE 1 Throw 600 times with a dice and calculate the probability of each outcome.

Simulate 600 times throwing a dice. Name your column **d**.

◀	1.1	*Doc <	~ ¹ 3	GRA	VD 🚺	×	
P	A d	В	С	D			
=	=randint(1						
1	6					Ī	
2	6						
3	1						
4	4						
5	3						
A	A d:=randint(1,6,600)						

Make a column **x** with the outcomes 1, 2, 3, 4, 5 and 6.

4	1.1	*Doc <	~ &	GRA	VD 🚺 🗙
P	A d	В	^C x	D	
=	=randint(1				
1	6		1		
2	6		2		
3	1		3		
4	4		4		
5	3		5		
F3					

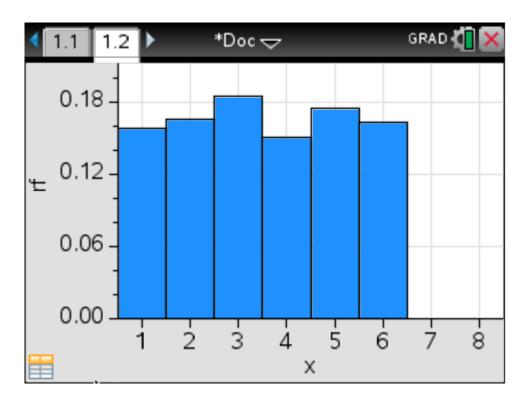
Make a frequency list **f** and go to the first free cell (here D1).

To give the frequencies we use : =countif(d,?=c1) ; enter. Than select this cell and go to MENU : 3 data : 3 fill to copy this formula to c2till c6.

•	1.1	*Doc <	~ ¹ 3		GRA	10 🚺	X
P	A d	В	C X		D f		
=	=randint(1						
1	6			1		95	
2	6			2		100	
3	1			3		111	
4	4			4		91	
5	3			5		105	
D1	=countif(d	,?=c1)				•	

•	A d	в	C x	□f	⊑ rf	F	G	Н	
=	=randint(1				='f/600*1.				
1	6		1	95	0.158333				
2	6		2	100	0.166667				
3	1		3	111	0.185				
4	4		4	91	0.151667				
5	3		5	105	0.175				
6	5		6	98	0.163333				
7	1								
8	3								
9	6								
10	2								
11	5								
<								>	~
J9									

Now we can calculate the relative frequencies (\mathbf{rf}) and for example make it visible in a graph.



Example 2 Simulate 20 families with 3 children and calculate the probability of having 2 girls.

4	1.1 1.2 2	.1 🕨 *Doc 🗸	~ ¹ 3	GRAD 🚺 🗙
•	A girl	В	С	D
=				
1	0			
2	3			
3	0			
4	1			
5	0			
A1	=sum(rand	int(0,1,3))		< ►

•	A girl	В	C x	□ f	E rf	F	G	H	
=					='f/(20.)				
1	0		0	7	0.35				
2	3		1	5	0.25				
3	0		2	3	0.15				
4	1		3	5	0.25				
5	0								
6	2								
7	1								
8	0								
9	1								
10	1								
11	2								
<									
D1	=countif(gi	rl ,?=c1)							

<u>Method 2</u> randint(0,1,20)

Use 3 lists ; one for the first child, one for the second child and one for the last child.

4	1.2 2.1 3.1 ▶ *Doc - GR/							
P	A	В	С	D				
=	=randint(0	=randint(0	=randint(0					
1	1	1	0					
2	0	0	0					
3	0	1	0					
4	1	0	0					
5	0	0	0					
A =	A =randint(0, 1, 20)							

Make a column 'girl' and calculate A+B+C.

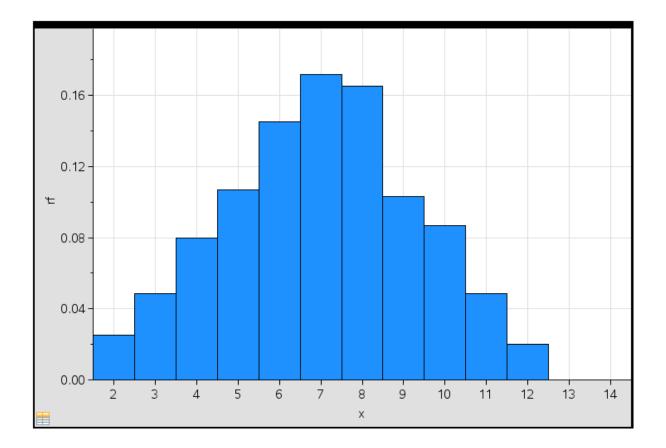
< 1.2 2.1 3.1 🕨 *Doc 🤝 😽 😽 GRAD 🚺						
•	A	В	С	D girl		
=	=randint(0	=randint(0	=randint(0	=a[]+b[]+		
1	1	1	0	2	2	
2	0	0	0	0		
3	0	1	0	1		
4	1	0	0	1		
5	0	0	0	0		
$D \mathbf{girl} = a[[]] + b[[]] + c[[]] \qquad \blacktriangleleft$						

Complete your spreadsheet.

•	A	В	С	D girl	Ex	F f	G rf	H
=	=randint(0	=randint(0	=randint(0	=a[]+b[]+o			='f/(20.)	
1	1	1	0	2	0	3	0.15	
2	0	0	0	0	1	7	0.35	
З	0	1	0	1	2	10	0.5	
4	1	0	0	1	3	0	0.	
5	0	0	0	0				
6	1	1	0	2				
7	1	1	0	2				
8	1	0	1	2				
9	1	0	0	1				
10	1	1	0	2				
11	0	0	1	1				
<								
	=countif(gi i	rl,?=e1)						

•	A	в	⊂ d	□x	⊑ f	F rf	G	ΗÊ
=	=randint(1	=randint(1	=a[]+b[]			='f/(600.)		
1	1	2	3	2	15	0.025		
2	6	4	10	3	29	0.048333		
З	1	6	7	4	48	0.08		
4	2	5	7	5	64	0.106667		
5	3	1	4	6	87	0.145		
6	2	6	8	7	103	0.171667		
7	4	4	8	8	99	0.165		
8	1	4	5	9	62	0.103333		
9	4	3	7	10	52	0.086667		
10	5	4	9	11	29	0.048333		
11	5	1	6	12	12	0.02		
≮ F9:1	F11							

EXAMPLE 3 Simulate throwing 600 times with two die and calculate the probability that the sum of the two die is 10 or more. Use the method of lists.



EXAMPLE 4 From a survey in 2008 is given that 59% of the Flemish people older than 18 do sports.

Simulate 300 times a group of 3 Flemish people and calculate the experimental probability that 0, 1, 2 or 3 persons of that group do sports. Generate 3 rows with zeros and ones where the one stands for 'do sport'. Keep in mind that 59% of the Flemish people do sport.

Example 5 From a survey in the secondary school is given that 20% of the students often chat during class and don't pay attention to the explanation of the teacher.

Simulate 300 times a group of 5 students.

- a) Calculate how many groups have no students that chat during the explanation of the teacher.
- b) Calculate how many groups only have one student that chat during the explanation of the teacher.